Correlated neuronal discharge rate and its implications for psychophysical performance

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SINGLE neurons can signal subtle changes in the sensory environment with surprising fidelity, often matching the perceptual sensitivity of trained psychophysical observers. This similarity poses an intriguing puzzle: why is psychophysical sensitivity not greater than that of single neurons? Pooling responses across neurons should average out noise in the activity of single cells, leading to substantially improved psychophysical performance. If, however, noise is correlated among these neurons, the beneficial effects of pooling would be diminished. To assess correlation within a pool, the responses of pairs of neurons were recorded simultaneously during repeated stimulus presentations. We report here that the observed covariation in spike count was relatively weak, the correlation coefficient averaging 0.12. A theoretical analysis revealed, however, that weak correlation can limit substantially the signalling capacity of the pool. In addition, theory suggests a relationship between neuronal responses and psychophysical decisions which may prove useful for identifying cell populations underlying specific perceptual capacities.

We obtained data from 100 pairs of neurons in the middle temporal visual area (MT, or V5) while three rhesus monkeys viewed random dot patterns presented on a video monitor. Because directionally selective neurons in MT supply signals for discriminating the direction of motion in these displays, this system provides an ideal opportunity to measure correlation within a pool of sensory neurons contributing to psychophysical performance. Action potentials were recorded using a single electrode and a spike sorting device which recognized individual

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stimulus condition tested. Throughout our analyses a response was considered to be the total number of action potentials recorded during presentation of a visual stimulus. A $\chi^2$ test of homogeneity showed that the correlation coefficients computed for a pair of neurons were independent of stimulus condition in 89% of the experiments ($P > 0.05$; correlation coefficients were first transformed to Fisher’s $z$ to conform to normality assumptions). Furthermore, we found no systematic difference in the average correlation coefficient between the two behavioural tasks (paired $t$-test, $P > 0.75$). We therefore combined data across stimulus conditions and tasks to compute a single correlation coefficient for each pair of neurons. To remove the influence of confounding variables such as stimulus strength, spike counts were converted to $z$-scores using the mean and standard deviation for repetitions of each stimulus type. We then calculated the correlation coefficient between ordered pairs of $z$-scores.

For the 100 pairs of MT neurons, the mean correlation coefficient was 0.12, a value significantly greater than zero ($t$-test, $P < 0.0001$). Furthermore, the correlation coefficient depended significantly on the difference in preferred direction of the two neurons. Figure 2a shows the distribution of correlation

**FIG. 1** Average responses of a pair of simultaneously recorded MT neurons during the fixation and discrimination tasks. Polar plots (a, c) are direction tuning curves measured during the fixation task for neuron 1 (a, b) and neuron 2 (c, d). For each data point, the angle indicates the direction of stimulus motion and the distance from the origin represents the average response (spikes per s) to that direction. Coherence–response functions (b, d) depict average responses to motion signals of increasing strength. Empty symbols indicate responses to preferred direction motion and filled symbols show responses to the opposite (null) direction. Error bars denote standard deviations.

**METHODS.** Our methods have been described previously. To summarize, direction tuning curves were measured with moving random dot patterns. The position of the dot pattern and the motion speed were set to stimulate the receptive fields of both neurons as well as possible. In the discrimination task, a specified percentage of dots in the visual display moved coherently in one direction while the remaining dots were plotted briefly at random locations, creating a masking motion noise. Monkeys received liquid rewards for reporting the direction of coherent motion correctly. Task difficulty was varied by changing the percentage of dots in coherent motion. On each trial, the direction of motion was either the preferred or null direction of the recorded neurons. If the preferred directions of the two neurons differed substantially, the axis of discrimination was set to the preferred-null axis of the best-responding neuron. In both the discrimination and fixation tasks, each stimulus condition was repeated 10–40 times in random order. Both discrimination and fixation data were obtained for 42 pairs of neurons; fixation data alone were obtained for the remaining pairs.

**FIG. 2** Frequency histograms of the correlation coefficients measured between pairs of MT neurons. **a**. Distribution of correlation coefficients for 52 pairs of neurons whose preferred directions differed by less than 90°. **b**. Distribution of coefficients for 13 pairs of neurons whose preferred directions differed by more than 90° and 35 pairs for which one neuron was not directional. Three analyses were done to control for artefactual sources of correlated responsiveness. First, we suppressed slow changes in responsiveness by renormalizing the standardized responses in blocks of 20 trials. This manipulation removed any yoked drift in overall responsiveness that might cause spurious correlation between the two neurons, but had no effect on the computed correlation coefficients (paired $t$-test, $P > 0.9$). To ensure that correlations were not driven entirely by outlier data points (resulting, perhaps, from brief lapses in the quality of isolation), we ‘pruned’ from each data set trials on which the response of either neuron was more than two standard deviations from that neuron’s mean response for a given stimulus condition. Pruning did not affect the correlation coefficients (paired $t$-test, $P > 0.4$).

Last, our random dot patterns typically are computed uniquely on each trial so that the monkey cannot solve the task by memorizing specific patterns of dots for each motion condition. This, however, introduces a small amount of variation among nominally identical stimuli that might give rise to spurious correlation. For four neuronal pairs, therefore, we obtained data using stimuli computed in the usual manner and then using a single predetermined random dot pattern for each stimulus condition (the difference in preferred directions was less than 45° for three pairs and was 103° for the remaining pair). Without stimulus-induced variance, the mean correlation coefficient remained significantly greater than 0 (paired $t$-test, $P = 0.005$). The correlation coefficients were similar with and without stimulus variation (means = 0.15 and 0.22, respectively), although our sample is too small to exclude the possibility of a moderate difference.

We accepted data only from experiments with excellent separability between the two templates and between each template and the background noise.

Responses were recorded during two behavioural tasks, fixation and discrimination. In the former, the monkeys maintained fixation while the visual stimulus was presented within the receptive fields of the two cells. We measured the directional tuning of each neuron and used these data to assess the degree of correlated responsiveness. In the discrimination task, the monkeys reported the direction of coherent motion embedded in a field of random motion noise (see Fig. 1 legend). These data allowed us to assess correlated responsiveness during performance of the discrimination task. Figure 1 illustrates the responses of a pair of MT neurons in the two tasks. Both cells responded selectively to the direction of coherent motion, but signalled direction with decreasing reliability as coherent motion was reduced.

For each pair, we computed the correlation coefficient, $r$, between the responses of the two neurons to multiple presentations of a given stimulus. This process was repeated for each
FIG. 3 Effect of pooling for different levels of correlation. a, Signal-to-noise ratio of the pooled average response as a function of increasing pool size, b. Covariation between individual responses and the pooled average response (ordinate) as a function of increasing pool size (abscissa). Each curve shows results for a particular correlation level within the pool (mean correlation, \( r = 0 \) to 0.5 in increments of 0.05). The dashed curves indicate the correlation levels that are most plausible from our physiological data. The curves represent analytical solutions to the equations presented below for \( M \) identically distributed neural signals. In the present context, each signal distribution represents the responses of a single neuron contributing to a sensory pool. The assumption of identically distributed signals, while overly simplified from real pools of neurons, is convenient computationally and does not influence our conclusions substantially. For \( a \), we calculate the signal-to-noise ratio of \( M \) summed signals, \( S/N \),

\[
S/N = \frac{\sum_{i=1}^{M} X_i}{\sigma_n}
\]

\[
= \frac{M \langle X \rangle}{\sqrt{\sum_{i=1}^{M} \sum_{j=1}^{M} \text{Cov}(X_i, X_j)}}
\]

\[
= \frac{M \langle X \rangle}{\sqrt{M \sigma^2 + M(M-1)r^2 \sigma^2}}
\]

where \( \sigma_n \) is the standard deviation of the sum and brackets denote expectation. Each curve depicts the \( S/N \) of the pool normalized to the \( S/N \) of a single neural signal. For large \( M \), improvement is limited by \( 1/\sqrt{M} \). For \( b \), we compute the expected correlation, \( \rho \), between one random signal, \( X_i \), and the sum of \( X_1 \ldots X_M \). The covariance can be written as

\[
\rho \sigma_1 \sigma_2 = \rho \sqrt{\sum_{i=1}^{M} \sum_{j=1}^{M} \text{Cov}(X_i, X_j)}
\]

\[
= \rho \sigma_n \sqrt{M \sigma^2 + M(M-1)\sigma^2}
\]

or in terms of products and their expectations

\[
\text{Cov}(X_i, \sum_{i=1}^{M} X_i) = \langle X_i \sum_{i=1}^{M} X_i \rangle - \langle X_i \rangle \langle \sum_{i=1}^{M} X_i \rangle
\]

\[
= \langle X_i^2 \rangle + \sum_{i=2}^{M} \langle X_i \rangle \langle X_j \rangle - \langle X_i \rangle \langle \sum_{i=1}^{M} X_i \rangle
\]

\[
= \sigma^2 + \sum_{i=2}^{M} \text{Cov}(X_i, X_j)
\]

\[
- \sigma^2 + (M-1) \sigma^2
\]

where \( \bar{r}_i \) is the average correlation coefficient between signal 1 and each of the other signals. Solving for \( \rho \) in equations (2) and (3) we obtain

\[
\rho = \frac{1 + (M-1)\bar{r}_i}{\sqrt{M + M(M-1)\bar{r}_i^2}}
\]

The correlation coefficient, \( \rho \), between a single random signal and the sum to which it contributes is plotted in \( b \). By analogy with real neuronal pools, this correlation could reflect the covariation between a single neuron's response and the outcome of a psychophysical decision governed by the summed signal, or decision variable. Even with arbitrarily large pools the correlation asymptotes at \( \sqrt{r_i} \).

coefficients for pairs of neurons whose preferred directions differed by less than 90 degrees, and Fig. 2b depicts the corresponding distribution for pairs that failed to meet this condition. The difference between the two distributions is highly significant (t-test, \( P < 0.001 \)). The correlation values in Fig. 2a agree well with similar measurements made in striate cortex of cats and inferotemporal cortex of monkeys.

Our data indicate that adjacent MT neurons covary weakly in their response to visual stimuli. Even such weak covariation places fundamental limits on the signal-to-noise ratio (S/N) of any stimulus represented in the activity of a pool of sensory neurons. Figure 3a shows the expected improvement in S/N conferred by signal averaging among neuronal pools of increasing size. If neurons within the pool are independent (\( r = 0 \)), then S/N should improve by the square root of their number. If neurons within the pool covary even weakly, however, S/N of the pooled response is limited, reaching an asymptote at \( r^{-1/2} \) times the S/N of a single neuron in the pool. Note that little increase in S/N is expected for pool sizes larger than 50-100 neurons. Thus, the beneficial effects of pooling are curtailed sharply by weak correlation, rendering more plausible the impressive sensitivity of single neurons relative to psychophysical threshold.

Because our data were recorded from adjacent neurons, we may have overestimated the average correlation in the pool if correlation declines with distance between neurons. Figure 3a shows, however, that S/N would reach an asymptotic limit near 100 neurons even if the average correlation within the pool were less than our measured value.

Weak covariation can lead to a covariation between the noisy responses of single neurons and psychophysical decisions. Figure 3b illustrates the trial-to-trial correlation expected between the responses of any single neuron and the pooled signals represented in Fig. 3a. If neurons within the pool are independent, the covariation of any one neuron with the pooled response must vanish with increasing pool size (\( r = 0 \)). If pairs of neurons covary even weakly, however, each neuron retains a covariation with the pooled average even for large pools. If psychophysical decisions are based on pooled signals like those in Fig. 3, near-threshold decisions should be correlated with the response fluctuations of single neurons within the pool.

We have in fact observed such covariation between neuronal responses and psychophysical decisions during performance on our direction discrimination task, and a similar phenomenon has been reported in the somatosensory system. Our analysis suggests that the covariation of single-neuron responses and psychophysical decisions, an observation that strains credulity at first glance, is a logical consequence of weakly correlated noise within the pool of sensory neurons leading to the decision. If such correlation is a general characteristic of neuronal pools underlying psychophysical performance, trial-to-trial covariation between neuronal responses and decisions may prove useful.
for identifying neurons that contribute to various perceptual capacities.

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